

# ESERCIZIO 5 - 20 punti

MAX(A[1..m])

if  $m=3$  then return MAX(A[1], A[2], A[3])

else

$m = m/3$

return MAX(MAX3(A[1..m]), MAX3(A[m+1]..2m), MAX3(A[2m+1..m]))

$$T(m) = \begin{cases} 1 & \text{se } m=3 \\ 3T(m/3) + c & \text{altrimenti} \end{cases}$$

$$T(m) = 3T(m/3) + c$$

$$T(m/3) = 3T(m/9) + c$$

$$T(m) = 3(3T(m/9) + c) + c$$

$$T(m/9) = 3T(m/27) + c$$

$$T(m) = 3(3(3T(m/27) + c) + c) + c$$

$$T(m) = 3^i T(m/3^i) + \sum_{j=0}^{i-1} 3^j \cdot c \Rightarrow T(m/3^i) = 1 \quad i = \log_3 m$$

$$T(m) = 3^{\log_3 m} T(1) + \sum_{j=0}^{\log_3 m - 1} 3^j \cdot c \Rightarrow T(m) = mT(1) + \frac{3^{\log_3 m} - 1}{3 - 1} \cdot c = mT(1) + \frac{m-1}{2} \cdot c$$

# ESERCIZIO 6 - 20 punti (50%)

A[1..m]

$m = 3m$  interi

DETERMINARE  $A_1 = \{a \in A : a \geq \frac{3m}{4}\}$

$A_2 = \{a \in A : a \leq \frac{3m}{4}\}$

ALL(A[1..m])

~~if  $m=3$  then~~  $j=0 \quad p=0$

$x = \text{SELECT}(A, 3m/4)$

for  $i=1$  to  $m$  do

if  $A[i] > x$

$A_2[j] = A[i] \quad j++$

else

$A_1[p] = A[i] \quad p++$