

④ $A_1 = \{ 5n^2 + n \log n + n^{3/2}, 4^{\log n}, n^2 + \log n^2, n \log 3^n, \frac{1}{4}n^2 + 6n\sqrt{n} \}$
 $A_2 = \{ n - \sqrt{n} \log n, \log n \log n, 10n + 3 \log \log^2 n, 4n + 2 \log n + 3\sqrt{n} \}$
 $A_3 = \{ 8n \log^3 n, n^5 \log n, \log(n! \cdot 2^n)^4, \log(n!) \log(n+2)^3 \}$
 $A_4 = \{ \log \log^2 n^3, \log \log n \}$
 $A_5 = \{ 3^n + 5^n \}, A_6 = \{ n! \}, A_7 = \{ 5 \cdot 2^n \}, A = \{ 4n^4 \}$

$$A_4 < A_2 < A_3 < A_1 < A_7 < A_8 < A_5 < A_6$$

Appunti: $4^{\log n} \Leftrightarrow 2^{2 \log n} \Leftrightarrow 2^{\log n^2} \Leftrightarrow n^2$, $8n \log^3 n \Leftrightarrow 2^3 n \log^3 n$
 $\Leftrightarrow 2^3 \frac{2^2 n^2}{3} \cdot \log^3 n \Leftrightarrow \frac{1}{3} \cdot 8 n \log^3 n \Leftrightarrow \frac{8}{3} n \log^3 n$
 $\log\left(\frac{n!}{2^n}\right)^4 \Leftrightarrow \log(n! \cdot 2^{-n})^4 \Leftrightarrow 4 \log n! - 4n$

⑤ $\log \log^2 n, \log n^4, 3 \log n^4, 7 \log^3 n, n^{\frac{1}{2} \log n}, 10^{\log n}, n^{\frac{\log n}{2}}, 10^{\frac{1}{2} \log n}, \sqrt[3]{n \log n}, \log \sqrt[3]{n}, \log^3 n$
 $n^5, (\log n)^n, n!, n^n$

⑥ $\Omega(f(n)) = \sqrt[3]{n} = \Theta(\sqrt[3]{n})$

$$\Omega(\sqrt[3]{n}) = \frac{1}{3} \log n = \Theta(\log n) = \Theta(1)$$

$$\Omega(n^2) = 2n^3 - 3n = \Theta(2n^3)$$

$$\Omega(n^{\frac{3}{2}}) = (n^3 + n) / (n \log^2 n + \log n) = \Theta(n^2)$$

$$\Omega(2^n) = (4^n) = \Theta(5^n)$$

$$\Omega(2^n) = 3(\log_3 n)^3 = \Theta(5^n)$$