

d) $\log\left(\frac{n}{\log n}\right) = \Theta(\log n)$

$\exists e_1, e_2, m_0 > 0 : e_1 \cdot \log n \leq \log \frac{n}{\log n} \leq e_2 \log n$

$\log \frac{n}{\log n} \geq e_1 \log n$

$\log(n \cdot (\log n)^{-1}) \geq e_1 \log n \Leftrightarrow \log n - \log \log n \geq e_1 \log n$

Non è possibile trovare costanti, efficienti, valide la seguente uguaglianza.

e) $5n\sqrt{n} \log n^2 + 10n^2 = \Theta(n^2)$

$\exists e_1, e_2, m_0 > 0 : e_1 \cdot n^2 \leq 5n\sqrt{n} \log n^2 + 10n^2 \leq e_2 \cdot n^2$

$5n\sqrt{n} \log n^2 + 10n^2 \geq e_1 \cdot n^2$

$2.5n\sqrt{n} \log n + 10n^2 \geq e_1 \cdot n^2 \Leftrightarrow e_1 = 1 \quad \forall n \geq 1$

$e_2 \cdot n^2 \geq 10n\sqrt{n} \log n + 10n^2 \Leftrightarrow e_2 \geq 10\sqrt{n} \log n + 10$

~~$e_2 \cdot n^2 \geq 10n^2 \log n + 10n^2$~~

~~$e_2 \geq 10 \log n + 10$~~

$e_2 n^2 \geq 10n(\sqrt{n} \log n + n) \Leftrightarrow e_2 n^2 \geq 10n(\sqrt{n} \log n + n)$

$10n(2n) \geq 10n(\sqrt{n} \log n + n) \text{ Verificate } \Leftrightarrow e_2 n^2 \geq 20n^2$

$e_2 = 20 \quad \forall n \geq 2$